Fiscal Unit/Academic Org
Administering College/Academic Group
Co-adminstering College/Academic Group
Semester Conversion Designation
Proposed Program/Plan Name
Type of Program/Plan
Program/Plan Code Abbreviation
Proposed Degree Title

Mathematics - D0671
Arts and Sciences
New Program/Plan
Mathematics Graduate Minor
Graduate minor
MATH-GM
Graduate Minor in Mathematics

## Credit Hour Explanation

| Program credit hour requirements |  | A) Number of credit hours <br> in current program (Quarter <br> credit hours) | B) Calculated result for <br> 2/3rds of current (Semester <br> credit hours) | C) Number of credit hours <br> required for proposed <br> program (Semester credit <br> hours) | D) Change in credit hours |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Total minimum credit hours required for <br> completion of program |  |  | 15 |  |  |
| Required credit hours <br> offered by the unit | Minimum |  |  | 15 |  |
|  | Maximum |  |  | 15 |  |
| Required credit hours <br> offered outside of the unit | Minimum |  |  |  |  |
|  | Maximum |  |  |  |  |
| Required prerequisite credit <br> hours not included above | Minimum |  |  |  |  |
|  | Maximum |  |  |  |  |

## Program Learning Goals

Note: these are required for all undergraduate degree programs and majors now, and will be required for all graduate and professional degree programs in 2012. Nonetheless, all programs are encouraged to complete these now.

## Program Learning Goals

- Students of the Graduate Minor acquire conceptual knowledge and problem solving skills in a wide range of mathematical subjects at a high level of abstraction, sophistication, and rigor.


## Assessment

Assessment plan includes student learning goals, how those goals are evaluated, and how the information collected is used to improve student learning. An assessment plan is required for undergraduate majors and degrees. Graduate and professional degree programs are encouraged to complete this now, but will not be required to do so until 2012.

Is this a degree program (undergraduate, graduate, or professional) or major proposal? No

## Program Specializations/Sub-Plans

If you do not specify a program specialization/sub-plan it will be assumed you are submitting this program for all program specializations/sub-plans.

## Pre-Major

Does this Program have a Pre-Major? No

## Attachments

## Comments

## Workflow Information

- Grad_Minor_Cover_Letter_2017_12_09.pdf: Cover Letter
(Letter from Program-offering Unit. Owner: Kerler,Thomas)
- Math_Grad_Minor_Proposal_2017_12_09_FINAL.pdf: Grad Minor Proposal
(Program Proposal. Owner: Kerler, Thomas)
- Math_Grad_Minor_AdvisingSheet_2017_12_09_FINAL.pdf: GM Advising Sheet
(Semester Advising Sheet(s). Owner: Kerler, Thomas)
- Math_Grad_Minor_Proposal_REVISED_2018_02_02.pdf: Revised Grad Minor Proposal
(Program Proposal. Owner: Kerler,Thomas)
- Math_Grad_Minor_AdvisingSheetDraft_REVISED_2018_02_02.pdf: Revised GM Advsing Sheet (Semester Advising Sheet(s). Owner: Kerler, Thomas)
- Revised Proposal and Advising Sheet were uploaded.

Revisions include:

- Minimum grades changed to ' $\mathrm{B}^{\prime}$ (redundant GPA requirement removed)
- Further explanation about the limitation to 5000,6000 level for the 9 -hour requirement added.
- Further explanation for accelerated curricula for students with candidacy time-limits added.
- Phase-In section added
- Miscellaneous edits and corrections of clerical errors. (by Kerler,Thomas on 02/02/2018 10:02 AM)
- Returned at the request of the program. (by Tott, Jill A on 01/24/2018 03:06 PM)

| Status | User(s) | Date/Time |  |
| :--- | :--- | :--- | :--- |
| Submitted | Kerler,Thomas | $12 / 09 / 2017$ 05:46 PM | Submitted for Approval |
| Approved | Husen,William J | $12 / 10 / 201708: 17 \mathrm{AM}$ | Unit Approval |
| Approved | Haddad,Deborah Moore | $12 / 10 / 2017$ 12:21 PM | College Approval |
| Revision Requested | Toft,Jill A | $01 / 24 / 2018$ 03:06 PM | GradSchool Approval |
| Submitted | Kerler,Thomas | $02 / 02 / 201810: 03 \mathrm{AM}$ | Submitted for Approval |
| Approved | Husen,William J | $02 / 02 / 201810: 03 \mathrm{AM}$ | Unit Approval |
| Approved | Haddad,Deborah Moore | $02 / 02 / 201812: 14 \mathrm{PM}$ | College Approval |
| Revision Requested | Toft,Jill A | $02 / 06 / 201811: 05 \mathrm{AM}$ | GradSchool Approval |
| Submitted | Husen,William J | $02 / 06 / 201811: 12 \mathrm{AM}$ | Submitted for Approval |
| Approved | Husen,William J | $02 / 06 / 201811: 12 \mathrm{AM}$ | Unit Approval |
| Pending Approval | Vankeerbergen,Bernadet <br> te Chantal | $02 / 06 / 2018$ 12:32 PM | Ad-Hoc Approval |
| Approved | Haddad,Deborah Moore | $02 / 06 / 201812: 33 \mathrm{PM}$ | College Approval |

RE: Proposal for a Graduate Minor in Mathematics.
Dear Colleagues,
On behalf of the Graduate Studies Committee (MGSC) of the Department of Mathematics I am pleased to submit a proposal for a new Graduate Minor in Mathematics via upload to the curriculum.osu.edu system. The proposal was approved by the MGSC on March $3^{\text {rd }}$ of this year and is support by our graduate faculty.

The uploaded proposal includes a rationale for the minor, a description of the proposed curriculum, an outline of the administrative arrangements to support the new minor, and enrollment plans and estimates. In addition, we have attached an advising sheet to be used by students and advisors of the minor.

Thank you very much for your consideration of our proposal.

Sincerely,


Thomas Kerler
Professor \& Vice-chair
Department of Mathematics

## Proposal for a Graduate Minor in Mathematics

The Graduate Studies Committee (MGSC) of the Department of Mathematics is proposing a new Graduate Minor in Mathematics (GM). The proposal was approved by the MGSC on March 3rd, 2017.

## Rationale

Graduate level mathematics courses have seen a steady increase in enrollment by graduate students from other programs at the Ohio State University (OSU) over the past years.

Notably, students from Computer Science and also other engineering departments frequently visit our master and doctoral level courses in topology and geometry, as problems in spatial modeling or topological data analysis require more and more sophisticated mathematical background. Students from Statistics routinely benefit from our advanced courses in probability theory and combinatorics. The Mathematics department also has a large faculty group in mathematical biology, and co-hosts the Mathematical Biosciences Institute. As a result, the department provides and teaches courses of great interest to students in life science departments who want to acquire the skills needed for mathematical modeling. Further examples include students from Philosophy attending logic and foundational courses, as well as students studying theoretical physics attending a broad range of graduate mathematics courses.

In recent times, one or two students each year manage to earn an MS degree in our program. However, by our estimate, many more students complete substantial graduate coursework in mathematics, without having this recognized in an official manner on their transcripts. There is also no good mechanism currently in place that would allow the mathematics department to advise these students on what mathematics courses would be appropriate and helpful to them.

With the proposed GM we aim to allow doctoral students from other programs, who have taken graduate level mathematics classes, but do not chose to obtain an MS degree, to have their advanced training in mathematics officially certified. The GM would create a framework to better guide such students through our course offerings, and, more generally, provide incentives for talented students to acquire knowledge in graduate level mathematics -- knowledge that is becoming increasingly relevant in many other areas of science.

## Eligibility

The proposed minor is open only to doctoral students in any graduate program at OSU. Other degree students (JD, MD, MS, MA, etc.) may be considered in special circumstance with the approval of the MGSC.

Students seeking to earn the GM further need to adhere to the enrollment, approval, and supervision process described in the sections on administration and enrollment below. Students also need to be in good academic standing with the university and their home programs.

## Proposed Curriculum and Requirements

In order to obtain a GM, a student is required to complete a minimum of $\mathbf{1 5}$ credit hours of approved graduate level mathematics courses. A complete set of these courses is listed in the appendix. An approved curriculum must further fulfill the following requirements:

- At least 4 mathematics courses at the 5000 -level or higher must be counted towards the GM requirements.
- All courses counted towards the GM must be passed with a grade of B or better, or an S for S/U graded courses, in compliance with Graduate School rules (Handbook, § 8.4).
- At most $\mathbf{3}$ credit hours of S/U graded courses may be counted towards the GM.
- At least $\mathbf{9}$ credit hours of the coursework counted towards the GM must be from letter graded mathematics courses at the 5000 or 6000 level.
- Group study courses (5194, 6194), internship courses (6191) and graduate research courses $(6998,6999,7998,8998,8999)$ are not allowed to count towards the GM.
- The study plan needs to be approved by the department.

S/U graded courses include independent studies courses, research and internship courses, as well as 7000 -level courses with the .02 -decimalization.

The requirements above allow nearly all graduate mathematics courses to count towards the GM, in order to respond to the wide range of mathematical topics found in quantitative disciplines, and the observed outside participation across our entire course offerings.

This is balanced with the stipulation that at least $60 \%$ of the coursework is from seriously graded courses with substantial skill training based on homework and exams, as well as the approval of study plans as described below. Courses beyond the 6000 level can be counted towards the 9 hours from the fourth item above only with special permission by the GSC. A respective petition to the GSC will require evidence that a 7000 or 8000 level course applies sufficiently rigorous skill-assessments and grading standards (in a manner comparable to a 5000 or 6000 level course), and that the student has adequate preparations to takes the course.

## Administration \& Approval of Study Plans

The administration of the GM will be chiefly the responsibility of the MGSC with logistic and clerical assistance by the Graduate Coordinator (GC) and further oversight by the Vice-chair for Graduate Studies (VCG).

To this end the MGSC will appoint each year a Graduate Minor Chair (GMC) from the Mathematics graduate faculty.

The principal responsibility of the GMC is the approval, on behalf of the MGSC, of study plans in accordance with the stated rules. Every student enrolling in the GM needs to confer with the GMC in order to discuss a plan of study in accordance with the general rules stated above. The GMC needs to approve the plan of study as well as coordinate later adjustments with the MGSC and the Graduate School.

The sample study plans listed below provide a guide for the GMC, and illustrate some types of plans that would be acceptable and beneficial for a broad range of students with reasonable mathematical background. More advanced options may require more careful evaluation of preparations, and more substantial deviations might require the GMC to consult with the MGSC.

The GMC may also coordinate such approvals with other graduate faculty in the department with better knowledge of a particular specialization. Also, the GMC may contact the GSC chair of the student's home department if there are doubts about the student's academic standing in the home program.

The course requirements will be recorded in the attached Advising Sheet which will be signed by the GMC upon completion, and collected by the GC. The VCG will be informed by the GC and GMC of the completion, and will approve the transcript designation form submission by the student on gradforms.osu.edu following the Graduate School process. The GMC will prepare annual reports of earned GM's and submit them to the MGSC.

## Enrollment

Before enrollment students need to have their study plan approved by the GMC. Previously taken courses may count towards the GM requirements. Students are asked to present the most recent Advising Report to the GMC for the proper evaluation of their background, the adequacy of the study plan, and their academic standing. The GMC will inform the MGSC chair, the VCG, and the GC of the approval.

The student follows the Graduate Schools online application procedures (via gradforms.osu.edu) and the VCG will approve the application subject to GMC approval and possible further departmental criteria. The online process involves approval by the Graduate School and electronic communication with the student and the student's advisor.

The department expects to enroll about 5-10 students in the GM during the initial phases of the program. The total number of students enrolled will be limited to 15 , mainly in order to be able to guarantee an orderly and sustainable process, both administratively and in terms of academic oversight. If there is a demand beyond this number, the department will reevaluate the administrative procedures and requirements for the GM.

The GC and VCG will also monitor long-time enrollment in the GM. If a student has not completed their GM requirements within 3 years of the initial application, the progress of the students will be reevaluated, which might result in disenrollment.

## Phase-In

The GM will be open to students who have started enrollment into their respective doctoral program no earlier than 13 months before the approval and inception of this degree program. (So, if, for example, the minor is approved by Autumn 2018, students should not have been enrolled before Autumn 2017). Retroactive course credits and exceptions are at the discretion of the MGSC.

## Sample Curricula

The following sample curricula were proposed by mathematics faculty after consultation with colleagues from other departments, and were considered as adequate by the MGSC. They may, thus, be considered as pre-approved assuming adequate preparation by the student. The curricula are organized by specialization of the student, and the separation into first and second year is meant only as a suggestion. Students whose programs require candidacy by the end of their second year are encouraged to either complete accelerated versions of these curricula in their first two years or, after candidacy, substitute 8999 hours in their program by GM electives with permission of their departments.

## 1. Engineering \& Physics

Background in advanced calculus and differential equations at the 4000-level.
First year: Math 5101, 5102
Second year: Math 5756, 5757
Third year: Math 5451

## 2. Economics \& Finance

Required background in calculus and probability theory.
First year: Math 5632
Second year: Math 5633, 5634

Third year: Math 5635, 5637

## 3. Philosophy \& Foundations

Background in advanced calculus and linear algebra.
First year: Math 5111, 5001
Second year: Math 5201, 5051
Third year: any Math 6001-6004 course

## 4. Life Science Departments

Background in calculus and life sciences.
First year: Math 5401, 5402
Second year: Math 5660, 5602
Third year: 5651 or 6601
(or any five of the six listed courses)

## 5. Statistics

Curricula have further sub-specializations depending on the student's interest. Doctoral students in statistics should have all prerequisite preparations. Foundational courses for all subspecializations:
(First and second year): Math 5201, 5202 and Math 5101
One or two additional courses depending on sub-specialization (third year):

- Discrete data analysis and optimization:

Math 6501, Math 5601, or Math 5603

- Shape analysis:

Math 5702, Math 6701, or Math 6702

- Nonparametric function estimation:

Math 5102, Math 5601, Math 5603

- Probability:

Math 6501, Math 6502, or Math 8250

## 6. Computer Science

Students are expected to have solid background in calculus and linear algebra. There are three proposed curricula depending on the student's sub-specialization and interests.

- Computational Geometry and Topology:

First year: Math 5702, 5801
Second year: Math 6501, 6502
Third year: Math 8710 or 8800

- Distributed computing/temporal logic:

First year: Math 5051 and any one of Math 6001-6004
Second year: Any one of Math 6001-6004
Third year: Math 6251, 6252

- Nonparametric function estimation:

First year: Math 5201, 5202
Second year: Math 6251, 6252
Third year: One of Math 6501, 6502, or 7211

## Attachments

- Cover Letter by VCG
- Advising Sheet


## Appendix: Mathematics Graduate Level Courses

| Course \# | Course Title | Credits |
| :---: | :---: | :---: |
| 5001 | Introduction to Set Theory | 3.0 |
| 5051 | Introduction to Mathematical Logic | 3.0 |
| 5101 | Linear Mathematics in Finite Dimensions | 3.0 |
| 5102 | Linear Mathematics in Infinite Dimensions | 3.0 |
| 5111 | Algebra I | 5.0 |
| 5112 | Algebra II | 5.0 |
| 5152 | Introduction to Number Theory with Applications | 3.0 |
| 5168 | Introduction to the Finite Element Method | 3.0 |
| 5201 | Introduction to Real Analysis I | 5.0 |
| 5202 | Introduction to Real Analysis II | 5.0 |
| 5221 | Introduction to Complex Analysis | 3.0 |
| 5251 | Complex Variables and Applications | 3.0 |
| 5401 | Applied Differential Equations I | 3.0 |
| 5402 | Applied Differential Equations II | 3.0 |
| 5421 | Mathematics of Infectious Disease Dynamics | 3.0 |
| 5451 | Calculus of Variations and Tensor Calculus | 3.0 |
| 5520 H | Honors Linear Algebra and Differential Equations | 5.0 |
| 5522H | Honors Complex Analysis | 5.0 |
| 5529 H | Honors Combinatorics | 5.0 |
| 5530 H | Honors Probability | 5.0 |
| 5540 H | Honors Differential Geometry | 5.0 |
| 5576 H | Honors Number Theory | 5.0 |
| 5590 H | Honors Abstract Algebra I | 5.0 |
| 5591 H | Honors Abstract Algebra II | 5.0 |
| 5601 | Essentials of Numerical Methods | 3.0 |
| 5602 | Computational Partial Differential Equations | 3.0 |
| 5603 | Numerical Linear Algebra | 3.0 |
| 5630 | Life Contingencies I | 3.0 |
| 5631 | Life Contingencies II | 3.0 |

Proposal for a Graduate Minor in Mathematics

| Course \# | Course Title | Credits |
| :---: | :---: | :---: |
| 5632 | Financial Economics for Actuaries | 3.0 |
| 5633 | Loss Models I | 3.0 |
| 5634 | Loss Models II | 3.0 |
| 5651 | Mathematical Modeling of Biological Processes | 3.0 |
| 5660 | Integrated Molecular and Cellular Biology for NonBiologists | 5.0 |
| 5702 | Curves and Surfaces in Euclidean Three Space | 3.0 |
| 5756 | Mathematical Methods in Relativity Theory I | 3.0 |
| 5757 | Mathematical Methods in Relativity Theory II | 3.0 |
| 5801 | General Topology and Knot Theory | 3.0 |
| 6001 | Advanced Mathematical Logic I: Proof Theory | 3.0 |
| 6002 | Advanced Mathematical Logic II: Model Theory | 3.0 |
| 6003 | Advanced Mathematical Logic III: Set Theory | 3.0 |
| 6004 | Advanced Mathematical Logic IV: Computability Theory | 3.0 |
| 6111 | Abstract Algebra I | 5.0 |
| 6112 | Abstract Algebra II | 5.0 |
| 6151 | Commutative Algebra | 3.0 |
| 6152 | Non-Commutative Algebra | 3.0 |
| 6193 | Individual Studies in Mathematics |  |
| 6211 | Real Analysis I | 5.0 |
| 6212 | Real Analysis II | 5.0 |
| 6221 | Complex Analysis I | 3.0 |
| 6222 | Complex Analysis II | 3.0 |
| 6251 | Theory of Probability I | 4.0 |
| 6252 | Theory of Probability II | 4.0 |
| 6411 | Ordinary Differential Equations I | 3.0 |
| 6451 | Partial Differential Equations I | 3.0 |
| 6501 | Combinatorics and Graph Theory I | 3.0 |
| 6502 | Combinatorics and Graph Theory II | 3.0 |
| 6601 | Numerical Methods in Scientific Computing I | 4.0 |
| 6602 | Numerical Methods in Scientific Computing II | 4.0 |
| 6701 | Differentiable Manifolds | 3.0 |
| 6702 | Differential Geometry | 3.0 |
| 6801 | Algebraic Topology I | 3.0 |
| 6802 | Algebraic Topology II | 3.0 |
| 7121.01 | Algebraic Number Theory | 3.0 |
| 7121.02 | Algebraic Number Theory | 3.0 |
| 7122.01 | Analytic Number Theory | 3.0 |
| 7122.02 | Analytic Number Theory | 3.0 |
| 7141 | Algebraic Geometry I | 3.0 |
| 7142 | Algebraic Geometry 2 | 3.0 |
| 7161.01 | Lie Algebras | 3.0 |

Proposal for a Graduate Minor in Mathematics

| Course \# | Course Title | Credits |
| :---: | :---: | :---: |
| 7161.02 | Lie Algebras | 3.0 |
| 7162.01 | Lie Groups and Representation Theory | 3.0 |
| 7162.02 | Lie Groups and Representation Theory | 3.0 |
| 7193 | Individual Studies in Mathematics |  |
| 7211 | Functional Analysis I | 3.0 |
| 7212 | Functional Analysis II | 3.0 |
| 7221.01 | Ergodic Theory I | 3.0 |
| 7221.02 | Ergodic Theory I | 3.0 |
| 7222.01 | Ergodic Theory II | 3.0 |
| 7222.02 | Ergodic Theory II | 3.0 |
| 7412.01 | Ordinary Differential Equations II | 3.0 |
| 7412.02 | Ordinary Differential Equations II | 3.0 |
| 7413 | Ordinary Differential Equations III | 3.0 |
| 7452 | Partial Differential Equations II | 3.0 |
| 7453 | Partial Differential Equations III | 3.0 |
| 7611 | Computational Partial Differential Equations I | 3.0 |
| 7612 | Computational Partial Differential Equations II | 3.0 |
| 7651 | Applied Complex Variables and Asymptotics I | 3.0 |
| 7652 | Applied Complex Variables and Asymptotics II | 3.0 |
| 7711 | Riemannian Geometry | 3.0 |
| 7721 | Kahler Geometry | 3.0 |
| 7811.01 | Homotopy Theory | 3.0 |
| 7811.02 | Homotopy Theory | 3.0 |
| 7851 | Differential Topology I | 3.0 |
| 7852 | Differential Topology II | 3.0 |
| 8000 | Topics in Foundations of Mathematics | 3.0 |
| 8110 | Topics in Algebra | 3.0 |
| 8120 | Topics in Number Theory | 3.0 |
| 8140 | Topics in Algebraic Geometry | 3.0 |
| 8160 | Topics in Representation Theory | 3.0 |
| 8210 | Topics in Real Analysis | 3.0 |
| 8220 | Topics in Complex Analysis | 3.0 |
| 8250 | Topics in Probability Theory | 3.0 |
| 8300 | Topics in Financial Mathematics | 3.0 |
| 8410 | Topics in Ordinary Differential Equations | 3.0 |
| 8420 | Topics in Partial Differential Equations | 3.0 |
| 8500 | Topics in Combinatorics | 3.0 |
| 8610 | Topics in Applied Mathematics | 3.0 |
| 8650 | Topics in Mathematical Biology | 3.0 |
| 8710 | Topics in Differential Geometry | 3.0 |
| 8750 | Topics in Lie Theory | 3.0 |
| 8800 | Topics in Topology | 3.0 |

## Graduate Minor in Mathematics <br> Advising Sheet

## Prerequisites:

- Doctoral student in an Ohio State graduate program.
- In good academic standing with the university and the home program.


## Requirements:

- Complete 15 credit hours of approved graduate level mathematics courses (consult webpage).
- At least 4 mathematics courses at the 5000 -level or higher must be counted towards the GM requirements.
- All courses counted towards the GM must be passed with a grade of B or better or an S for S/U graded courses.
- At most $\mathbf{3}$ credit hours of approved S/U graded courses may be counted towards the GM.
- At least 9 credit hours of the coursework counted towards the GM must be from letter graded mathematics courses at the 5000 or 6000 level.


## Study Plan:

The study plan needs to be completed by the student with approval of the Graduate Minor Chair (GMC) before enrolling. An Advising Report should be presented to the GMC. Further the form needs to be completed with grades and adjustments and signed by the GMC for the final approval of the minor transcript designation.

|  | Course \# | Abbr Title | Semester/Year | Credit Hrs | Grade |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |
| 2 |  |  |  |  |  |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |
|  |  |  |  | Tast |  |
|  |  |  |  |  | GPA |

## Approval:

Graduate Minor Form - GMC Approval (Study Plan \& Enrollment):
$\qquad$ Date:

Graduate Minor Transcript Designation - GMC Approval (Grades \& Requirements):
$\qquad$ Date:

## Suggested Curricula

1. Engineering \& Physics

First year: Math 5101, 5102
Second year: Math 5756, 5757
Third year: Math 5451
2. Economics \& Finance

First year: Math 5632,
Second year: Math 5633, 5634
Third year: Math 5635, 5637
3. Philosophy \& Foundations

First year: Math 5111, 5001
Second year: Math 5201, 5051
Third year: any Math 6001-6004 course
4. Life Science Departments

First year: Math 5401, 5402
Second year: Math 5660, 5602
Third year: 5651 or 6601
(or any five of the six listed courses)
5. Statistics

- Discrete data analysis and optimization:

Math 6501, Math 5601, or Math 5603

- Shape analysis:

Math 5702, Math 6701, or Math 6702

- Nonparametric function estimation:

Math 5102, Math 5601, Math 5603

- Probability:

Math 6501, Math 6502, or Math 8250
6. Computer Science

- Computational Geometry and Topology:

First year: Math 5702, 5801
Second year: Math 6501, 6502
Third year: Math 8710 or 8800

- Distributed computing/temporal logic:

First year: Math 5051 and any of Math 6001-6004
Second year: Math 6251, 6252

- Nonparametric function estimation:

First year: Math 5201, 5202
Second year: Math 6251, 6252
Third year: One of Math 6501, 6502, or 7211

